

ARIKETAK. LEHENENGO ZATIA (1, 2, 3 . Gaiak).

- 1) Oinarritzko Zirkuitu digitalak erabiliz, kotxearen segurtasun-uhalerako alarma sistema diseinatu ezazu. Sistemak detektatu behar izango du kotxea martxan jarri dugunean eta segurtasun-uhala jarrita ez dugunean.

$$f = \bar{A}B$$

- 2) Oinarritzko zirkuitu digitalak erabiliz, etxearen gelarako arrotz-detektagailu sistema diseinatu ezazu. Horretarako sentsoareak gelako bi leihoetan eta atean izango ditugu. Leihoa edo atea zabaltzen direnean sentsoare hauek maila altuko irteera ematen dute

$$f = A + B + C$$

- 3) Garatu ondorengo adierazpenak, modu kanonikoa lortu arte:

$$f_1 = \bar{A}C + \bar{A}CD + \bar{A}BCD \quad \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}BC\bar{D} + \bar{A}BCD$$

$$f_2 = \bar{A}C\bar{D} + AC + ABC \quad \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}BC\bar{D} + \bar{A}BCD$$

$$f_3 = \bar{A}B + AC \quad \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC$$

$$f_4 = (\bar{B} + \bar{D})(\bar{B} + A)(C + \bar{D})(\bar{D} + A)$$

$$f_5 = (X_1 + X_3)(X_3 + X_2X_4) + (X_3X_5 + (X_1 + X_4)(X_2 + \bar{X}_3))$$

- 4) Karnaugh-en mapak erabiliz, adierazi eta sinplifika itzazu ondorengo funtzioak.

a) $f_1 = (1, 3, 9, 10, 12, 13, 14, 15)_m \quad \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}C\bar{D} + \bar{A}B$

b) $f_2 = (0, 2, 3, 4, 5, 7, 8, 10, 11)_m \quad \bar{B}C + \bar{A}B\bar{D} + \bar{A}\bar{C}\bar{D} + \bar{B}\bar{C}\bar{D}$

c) $f_3 = (1, 6, 7)_m \quad AB + \bar{A}\bar{B}C$

d) $f_4 = (0, 1, 6)_M \quad (A + B)(\bar{A} + \bar{B} + C)$

e) $f_5 = (0, 1, 2, 3, 7, 8, 9, 11, 15)_m + K(6, 12) \quad \bar{A}\bar{B} + C\bar{D} + \bar{A}C + \bar{A}\bar{C}\bar{D} + \bar{A}\bar{B}C$

f) $f_6 = (3, 6, 7, 8, 10)_m + K(12, 13, 14) \quad \bar{A}C\bar{D} + \bar{A}B\bar{C} + \bar{A}\bar{D} + \bar{A}B\bar{C}$

g) $f_7 = (0, 1, 4, 5, 7, 8, 10, 15)_m + K(2, 6, 14) \quad \bar{A}\bar{E} + BC + C\bar{D} + \bar{A}\bar{B}\bar{D}$

h) $f_8 = (0, 1, 4, 5, 6, 7, 12, 13, 14, 16, 17, 28, 29)_m + K(10, 11, 22, 23, 25, 26, 30, 31)$

$$\bar{A}C\bar{D} + \bar{A}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{B}\bar{C}\bar{D} + \bar{B}\bar{D}\bar{E}$$

- 5) NAND logika erabiliz osa itzazu ondorengo adierazpenak:

a) $ABC + DE$

b) $ABC + \bar{D} + \bar{E}$

c) ABC

d) $\bar{A}\bar{B} + \bar{C}\bar{D}$

e) $(A + B)(C + D)$

f) $AB[C(DE + \bar{A}B) + \bar{B}C\bar{E}]$

g) $B(CDE + \bar{E}FG)(\bar{A}B + C)$

- 6) Familia logiko ezberdinen ezaugarriak adierazgarrienak ondorengo taulan agertzen dira. Lor itzazu zarata-tarteak eta fan-out:

	TTL	TTL LS	TTL ALS	CMOS
V _{cc}	5V	5V	5V	3V-18V
V _{IH}	2.0	2.0	2.0	3.5
V _{IL}	0.8	0.8	0.8	1.5
V _{OH}	2.4	2.7	2.7	4.5
V _{OL}	0.4	0.5	0.4	0.5
I _{IH} μ A	40	20	20	0.005
I _{IL} mA	-1.6	-0.36	-0.2	-0.005 μ A
I _{OH} μ A	-400	-400	-400	-360
I _{OL} mA	16	8	4	4

- 7) Zirkuitu inpresio batetan TTL Standar-arekin egindako txip bat daukagu. Posiblea litzateke Txip horren ordeztu TTL LS edo TTL AS txip bat jartzea?

- 8) Bidegurutze batetako semaforoen funtzionamendua, ondorengo baldintzetan datza:

- A kalean kotxe bat baldin badago, orduan kale horretako semaforoa berde dago.
- B kalean kotxe bat baldin badago, orduan kale horretako semaforoa berde egongo da baldin eta A kalean kotxerik ez badaude.
- C kalean kotxe bat baldin badago, orduan kale horretako semaforoa berde egongo da baldin eta A eta B kaleetan kotxerik ez badaude.
- Kotxerik ez badaude, semaforo guztiak gorri daude.

Egitaula erabiliz, adieraz ezazu antolaketa honi dagokion funtzio logikoa (gorri = 1).

- 9) Entrepresa baten akzioak ondoren adierazten den moduan banatuta dituzte lau bazkideen artean:

$$A = 35\% \quad B = 30\% \quad C = 25\% \quad D = 10\%$$

Proposamen bat hautatu nahi denean, botuen arabera aurrera joango den ala ez jakiteko diseinatu ezazu funtzio logikoa.

$$Y = AB + AC + BC$$

- 10) Prozesu kimikoak egiten diren entrepresa batetan, hiru elementu kimiko ezberdin erabiltzen dira. Hiru elementu hauek hiru biltegi ezberdinetan gordetzen dira. Biltegi bakoitzean, elementu bakoitzaren maila adierazteko sensore bat dago. Likidoaren maila, adierazitako puntu baten azpitik dagoenean, sensoreak tentsio altua sortarazten du.

$$Y = \bar{A}BC + A\bar{B}C + AB$$

Biltegi bakoitzean elementu kimiko bakoitzaren maila, monitore batetan ikusgarri izan dadin, diseinatu ezazu zirkuitu bat, zeinak seinale bat emago duen bi biltegien maila, adierazitako puntuaren azpitik agertzen denean.

- 11) Diseinatu ezazu lau aldagai dituen zirkuitu logiko bat, zeinak 1 sortuko duen irteeran, sarreran hiru aldagai 1 direnean.

$$Y = BCD + ACD + ABD + ABC$$

- 12) Igogailu baten funtzionamenduan akatsik dagoen, detektatzen duen sistema diseinatu nahi da, zeinak ondoko baldintzak bete behar dituen:

- Igogailua matxan jartzen denean, atea itxita egon behar da.
- Hutsik badago eta eskaerarik ez badago, ez da mugitu behar.
- Geldirik badago, atea zabalik.

$$\bar{A}\bar{B} + AB + A\bar{C}\bar{D}$$

- 13) Zirkuitu logiko batek, 5 sarbide eta irtenbide 1 du. Bost sarbidetatik, lauk digito hamartar bat adieraten dute eta bostgarrena kontrolerako digitoa da. Kontrol-digito hau 0 logikoan dagoenean, irteera 0 logikoa izango da hamartarra zenbaki bikoitia baldin bada, eta irteera 1 izango da bakoitia baldin bada. Kontrol-digitoa 1 logikoan dagoenean, irteera 0 izango da, sarrera hiruren anizkoitza denean. Diseinatu ezazu zirkuitua.

ARISKEITÄT. LEHRENERGASO HANTA(1,2,3. Garsch) -001

- 1) A → segentes, chete
B → netken, gars

A	B	F
0	0	0
0	1	1
1	0	0
1	1	0

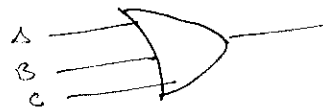
~~$f = \bar{A}B$~~

$$f = \bar{A}B$$

- 2) A → 1 lehnem
B → 2 lehnem
C → wten

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

$$f = A + B + C$$



- 4) Karnaughven bider simplifkato

a) $f_1 = (1, 3, 5, 10, 12, 13, 14, 15)_m$

0001
0011
1001
1010
1100
1101
1011
1111

$$\bar{A}\bar{B}D + A\bar{C}D + AC\bar{D} + AB$$

AB \ CD	00	01	11	10
00		1	1	
01				
11	1	1	1	1
10		1		1

$$(A\bar{B}\bar{C}D + A\bar{B}CD + A\bar{B}C\bar{D} + A\bar{B}CD)$$

b) $f_2 = (0, 2, 3, 4, 5, 7, 8, 10, 11)_m$

0000
0010
0011
0100
0101
0111
1000
1001
1010
1011

AB \ CD	00	01	11	10
00	1		1	1
01	1	1	1	
11				
10	1		1	1

$$\bar{B}C + \bar{A}BD + \bar{A}C\bar{D} + \bar{B}C\bar{D}$$

c) $f_3 = (1, 6, 7)_m$

001
110
111

AB \ C	0	1
00		1
01		
11	1	1
10		

$$AB + \bar{A}\bar{B}C$$

$$3) f_1 = \begin{matrix} 0000 & 1001 & 0111 \\ 0001 & 1101 & \\ 0100 & & \\ 0101 & & \end{matrix}$$

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + \bar{A}B\bar{C}D$$

$$f_2 = \begin{matrix} 0000 & 1010 & 1111 \\ 0100 & 1011 & 1111 \\ & 1110 & \\ & 1111 & \end{matrix}$$

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D$$

$$f_3 = \begin{matrix} 0100 & 1010 \\ 0101 & 1011 \\ 0110 & 1110 \\ 0111 & 1111 \end{matrix} \quad \begin{matrix} 010 & 101 \\ 011 & 111 \end{matrix}$$

$$\bar{A}B\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}\bar{C}$$

$$f_4 = \begin{matrix} 0101 & 0100 & 0001 & 0000 \\ 0110 & 0110 & 0101 & 0011 \\ 1101 & 0110 & 1001 & 0101 \\ 1111 & 0111 & 1101 & 0111 \end{matrix} \quad \Pi(1, 3, 4, 5, 6, 7, 9, 13, 14)$$

$$(A+B+C+D)(A+B+C+\bar{D})(\bar{A}+\bar{B}+C+D)(\bar{A}+\bar{B}+C+\bar{D})(A+\bar{B}+C+D)(A+\bar{B}+C+\bar{D})(\bar{A}+\bar{B}+C+D)(\bar{A}+\bar{B}+C+\bar{D})$$

$$f_5 = \bar{K}_3 \cdot \bar{K}_2 \cdot K_4 \cdot \bar{K}_3 (\bar{K}_2 + K_4)$$

$$4) f_4 = (0, 1, 6)M$$

$$\begin{matrix} 000 \\ 001 \\ 110 \end{matrix}$$

AB	0	1
00	0	0
01		
11	0	
10		

$$\bar{A}\bar{B} + \bar{A}B\bar{C}$$

$$(A+B)(\bar{A}+\bar{B}+C)$$

$$9) A=35\% \quad B=30\% \quad C=25\% \quad D=10\%$$

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$$\Sigma(6, 7, 10, 11, 12, 13, 14, 15)$$

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$\bar{A}\bar{B}C(\bar{D}+D) + A\bar{B}C(\bar{D}+D) + \bar{A}\bar{B}\bar{C}(\bar{D}+D) + A\bar{B}\bar{C}(\bar{D}+D)$$

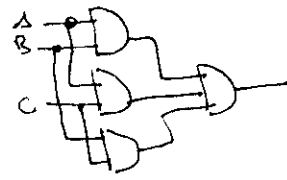
$$\bar{A}\bar{B}C + A\bar{B}C + \bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C}$$

$$\bar{A}\bar{B}C + A\bar{B}C + \bar{A}\bar{B}$$

$$B(A+\bar{A}) + A\bar{B}C$$

$$B\bar{A} + BC + A\bar{B}C$$

$$A(B+\bar{B}C) \quad \boxed{A\bar{B} + AC + BC}$$



3) A → kotxe → berde
er → gwr

B → ~~[kotxe → berde]~~ kotxe → A gwr → berde

C → kotxe → A gwr → B kotxe

A → kotxe → berde

B → kotxe
A kotxe er | berde

C → kotxe
A kotxe er | berde
B kotxe er

Kotxe/er → gwr

gwr = 1
berde = 0

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

0 → kotxe er
1 → kotxe/ai

A	B	C	S _A	S _B	S _C
0	0	0	1	1	1
0	0	1	1	1	0
0	1	0	1	0	0
0	1	1	1	0	1
1	0	0	0	1	1
1	0	1	0	1	1
1	1	0	0	1	1
1	1	1	0	1	1

$$S_A = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC$$

$$S_B = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C} + A\bar{B}C + A\bar{B}\bar{C} + A\bar{B}C$$

$$S_C = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C + AB\bar{C} + ABC$$

$$S_C = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C + AB\bar{C} + ABC$$

1) Bi seguratasun uhalekin.

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	0

$$\bar{A}\bar{B}C + \bar{A}BC + A\bar{B}C$$

$$\bar{A}(\bar{B}C + BC) + AC(\bar{B} + B)$$

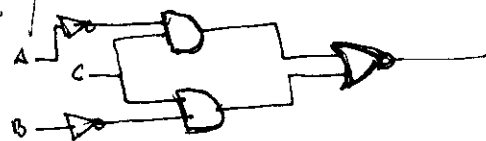
$$\bar{A}C(\bar{B} + B) + AC$$

$$C(\bar{A} + A) \rightarrow F = C$$

$$\bar{A}[C(\bar{B} + B)] + A\bar{B}C$$

$$\bar{A}C + A\bar{B}C$$

$$C(\bar{A} + A\bar{B}) \quad \boxed{C\bar{A} + C\bar{B}}$$



$$8) \bar{A}\bar{B}(\bar{C} + C) + \bar{A}[B(\bar{C} + C)]$$

$$\bar{A}(\bar{B} + B) \rightarrow \boxed{F = \bar{A}} \quad S_A$$

$$\bar{A}\bar{B}(\bar{C} + C) + A[\bar{B}(\bar{C} + C)] + AB(\bar{C} + C)$$

$$\bar{A}\bar{B} + A\bar{B} + AB \quad \bar{A}\bar{B} + A \quad \boxed{F = \bar{A} + B} \quad S_B$$

$$(\bar{A}\bar{B}(\bar{B} + B) + A(\bar{B}C + \bar{B}\bar{C}) + AB(\bar{C} + C))$$

$$\bar{A}\bar{B} + AC + AB$$

$$\bar{A}\bar{B}(\bar{B} + B) + BC(\bar{A} + A) + A\bar{B}(\bar{B} + B) + A\bar{B}C$$

$$\bar{A}\bar{B} + BC + A\bar{B} + A\bar{B}C$$

$$C(\bar{B} + A\bar{B}) \rightarrow C\bar{B} + CA$$

$$\bar{A}\bar{B} + A\bar{B} + AC + BC$$

$$\bar{A}\bar{B} + A(\bar{B} + C) + BC$$

$$A + \bar{B} + BC \quad \boxed{F = A + \bar{B} + B} \quad S_C$$

10) $A \rightarrow \text{behave} \rightarrow 1$

$B \rightarrow \text{behave} \rightarrow 1$

$C \rightarrow \text{behave} \rightarrow 1$

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

$$f = \bar{A}BC + A\bar{B}C + AB\bar{C} + ABC$$

$$\bar{A}BC + A\bar{B}C + AB\bar{C} + ABC$$

$$f = AB + AC + BC$$

11)

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$$\bar{A}BCD + A\bar{B}CD + AB\bar{C}D + ABC\bar{D} + ABCD$$

$$f = BCD + ACD + ABD + ABC$$

12) $\left. \begin{array}{l} \text{nicht an. ansteigende} \\ \text{nutz. ansteigend} \end{array} \right\} \rightarrow \text{selb.}$

4. e) $f = (0, 1, 2, 3, 7, 8, 9, 11, 15)_m + K(6, 12)$

0000
0001
0010
0011
0111
1000
1001
1011
1111
0110
1100

AB \ CD	00	01	11	10
00	1	1	1	1
01			1	
11	1	1	1	
10	1	1	1	

$$\bar{A}\bar{B} + CD + \bar{A}C + A\bar{C}\bar{D} + A\bar{B}\bar{C}$$

f) $f = (3, 6, 7, 8, 10)_m + K(12, 13, 14)$

0011
0110
0111
1000
1010
1100
1101
1110

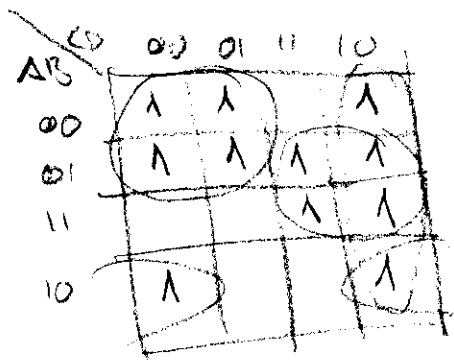
AB \ CD	00	01	11	10
00			1	
01			1	1
11	1	1		1
10	1			1

$$\bar{A}CD + \bar{A}BC + A\bar{D} + AB\bar{C}$$

AC + AB

4) a) $I_1 = (0, 1, 4, 5, 7, 8, 10, 15) \sim K(2, 6, 14)$

- 0000
- 0001
- 0100
- 0101
- 0111
- 1000
- 1010
- 1111
- 0010
- 0110
- 1110

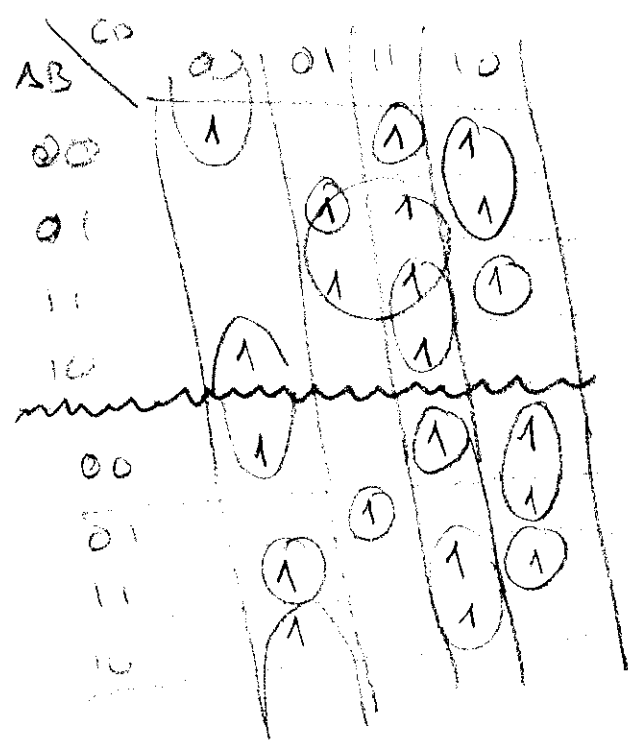


$$\bar{A}\bar{C} + BC + C\bar{D} + A\bar{B}\bar{D}$$

b) $I_2 = (0, 1, 4, 5, 6, 7, 12, 13, 14, 16, 17, 28, 29) \sim K(10, 11, 22, 23, 25, 26, 30, 31)$

2, 3, 8, 9, 10, 11, 15, 18, 19, 20, 21, 27, 29

- 0 00000 00010 10
- 1 00001 01011 11
- 4 00000 10110 22
- 5 00101 10111 23
- 6 00110 11001 25
- 7 00111 11010 26
- 12 01000 11110 30
- 13 01001 11111 31
- 16 10000
- 17 10001
- 28 11100
- 29 11101



$E=0$

$E=1$

$$\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D}$$

$$\bar{A}\bar{C}\bar{D} + A\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + \bar{B}\bar{C}\bar{D} + B\bar{C}\bar{D}$$

12) Aussagen bilden elementare
 hultik oder exklusive en \rightarrow gold?
 gold \rightarrow atre, hultik

Aussagen = 1

A	B	C	D	F
0	0	0	0	
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	
0	1	0	1	
0	1	1	0	
0	1	1	1	
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	

- A \rightarrow nutren = 1
- B \rightarrow atre, hultik = 1
- C \rightarrow hultik = 0
- D \rightarrow exklusive = 1

- 12) $A \rightarrow \text{master} = 1$
 $B \rightarrow \text{alter zulässig} = 1$
 $C \rightarrow \text{hutsik} = 0$
 $D \rightarrow \text{elakra} = 1$

$\backslash CD$	00	01	11	10
AB				
00				
01	0	0	0	0
11				
10		0	0	0

A	B	C	D	F
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

1 \rightarrow erlaubt
 0 \rightarrow nicht erlaubt

$\backslash CD$	00	01	11	10
AB				
00	1	1	1	1
01				
11	1	1	1	1
10	1			

$$\bar{A}\bar{B} + A\bar{B} + A\bar{C}\bar{D}$$

$$(A + \bar{B})(\bar{A} + B + \bar{D})(\bar{A} + B + \bar{C})$$

- 13) $A \ B \ C \ D \ E \ F$

digitale hamster
 kontrol
 digital

Kontrolle = 0 / orchen F = 0
 hamster = bitakt

Kontrolle = 0
 hamster = bitakt / orchen F = 1

Kontrolle = 1 / orchen F = 0
 schein = 3.7

$A \ B \ C \ D$	$E=0$	$E=1$
0000	X	X
0001	1	X
0010	0	X
0011	1	0
0100	0	X
0101	1	X
0110	0	0
0111	1	X
1000	0	X
1001	1	0
1010	0	X
1011	1	X
1100	0	0
1101	1	X
1110	0	X
1111	1	0

$\backslash CD$	00	01	11	10
AB				
00	X	1	1	0
01	0	1	1	0
11	0	1	1	0
10	0	1	1	0

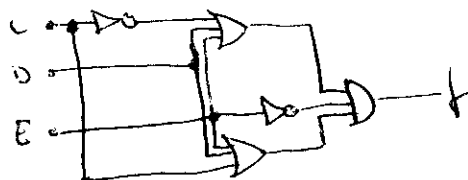
$E=0$

$\backslash CD$	00	01	11	10
AB				
00	X	X	0	X
01	X	X	X	0
11	0	X	0	X
10	X	0	X	X

$E=1$

$$F = \bar{D}\bar{E} + [\bar{B}\bar{D} + \bar{A}\bar{C} + A\bar{B}\bar{C} + B\bar{C}\bar{D} + A\bar{B}\bar{C} + \bar{A}\bar{B}\bar{D}]$$

$F = (\text{Kontrolle}) \vee (\text{Kontrolle}) \vee (\text{Kontrolle}) \vee (\text{Kontrolle}) \vee (\text{Kontrolle}) \vee (\text{Kontrolle}) \vee (\text{Kontrolle}) \vee (\text{Kontrolle})$



6) Zereke. berkeke

$$\text{TL} \quad V_{NH} = 0.4V$$

$$V_{NL} = 0.4V$$

$$f_{out} = 10 \text{ kHz}$$

$$\text{TL LS} \quad V_{NH} = 0.2V$$

$$V_{NL} = 0.3V$$

$$f_{out} = 20 \text{ kHz}$$

$$\text{TL SLS} \quad V_{NH} = 0.2V$$

$$V_{NL} = 0.4V$$

$$f_{out} = 10 \text{ kHz}$$

$$\text{CMOS} \quad V_{NH} = 1V$$

$$V_{NL} = 1V$$

$$f_{out} = 12 \text{ kHz}$$

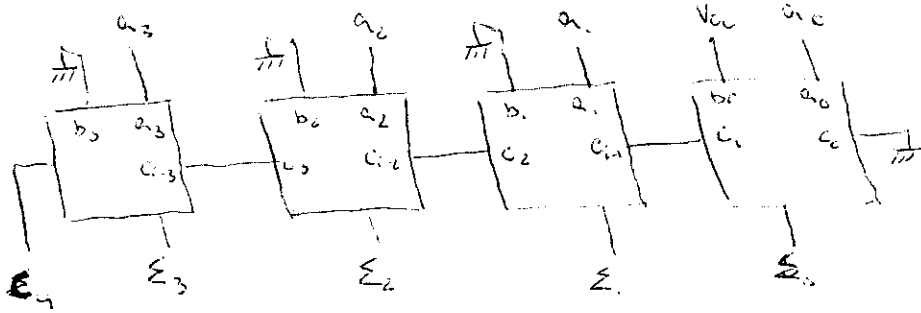
$$V_{NH} = V_{out \max} - V_{out \min}$$

$$V_{NL} = V_{in \max} - V_{in \min}$$

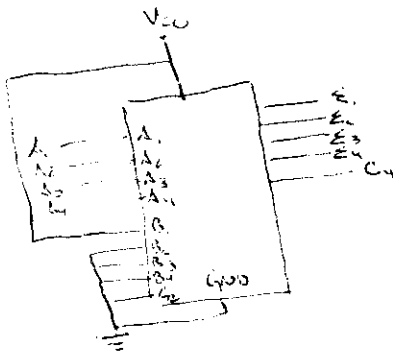
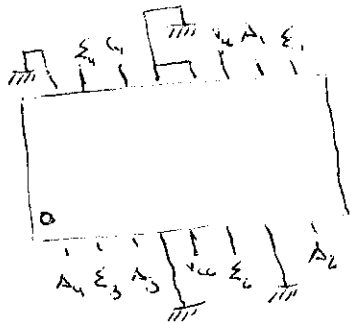
1) TL estenderaren bolson TL LS edo TL SS?

Bas Seisera markat berdinak dira bira berdinak

15)



7483 integrator exhibit



15) A-B interaction

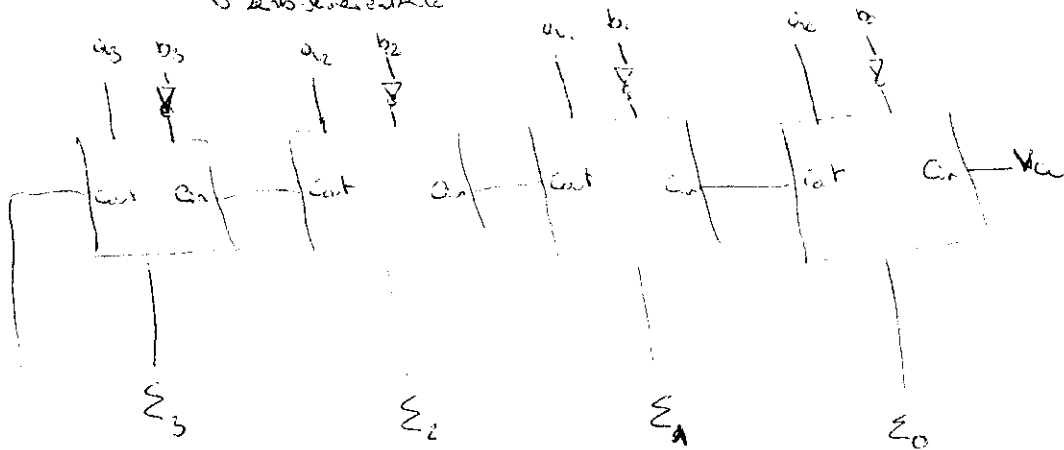
24. osiguranje

$A \cdot B < 0$ → electric wavelets
in led out parts

$$\lambda_3 = \lambda + (\sqrt{3} + 1)$$

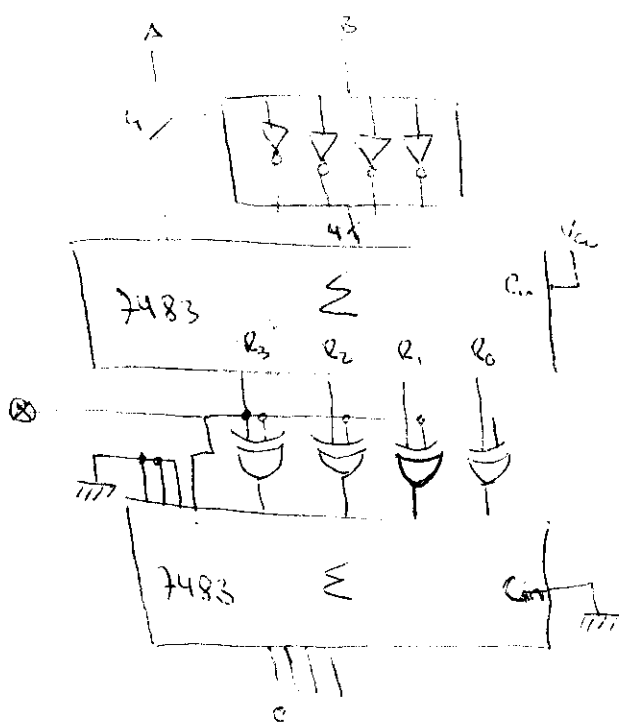
4 digits \rightarrow 1 server entry

3. Verb-lexeme entziffern



$\Sigma_3 \rightarrow$ Operation
 \rightarrow Association

Σ_3 ist negativ definit, die zugehörigen Eigenwerte des DSS-Behalters.

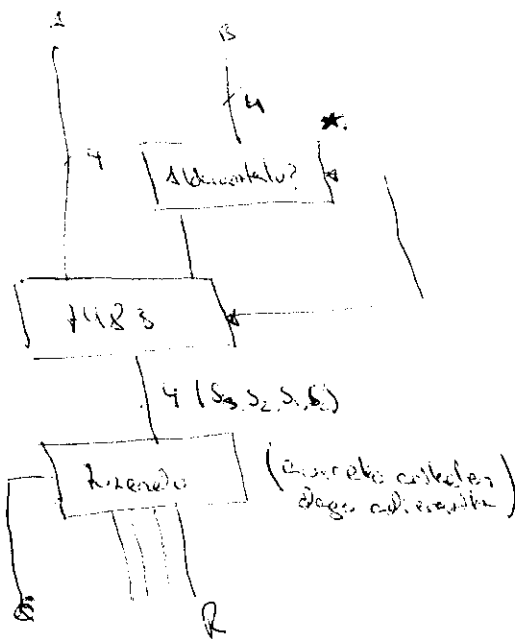


R_3	R_2	Aldeventu	Finale
0	0	0 er	
0	1	1 er	
1	0	1 hal	
1	1	0 bai	

16) $A, B \geq 0$ beide a_3, b_3 rechtsbittig

$A, B \in [-8, 7]$

Wort bezeichn. erhaltet, overflow neu gesteuert (adib: 2+3.16)



Erhaltet/Verändert

* $b_3 \oplus [S/R]$

b_3	\bar{S}/R	
0	0	0
0	1	1
1	0	1
1	1	0

Overflow erkennen

a_3	b_3	S_3	Overflow
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	0

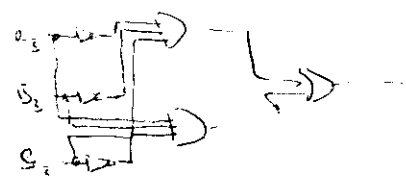
beide 0 sind beide 1

beide 1 sind beide 0

$S=0$ beide 0 sind beide 1

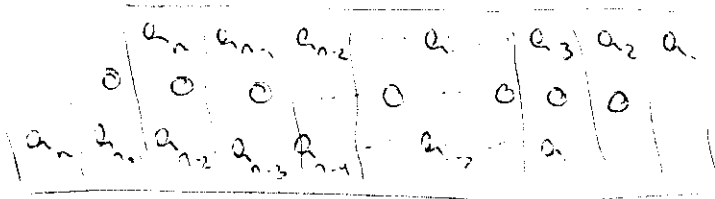
$S=1$ beide 1 sind beide 0

$$OV = \bar{a}_3 \bar{b}_3 S_3 + a_3 b_3 \bar{S}_3$$



17) n bit ripple carry

$$a_n a_{n-1} a_{n-2} \dots a_1 \dots a_3 a_2 a_1$$



$$R_{n+3} \quad R_{n+2} \quad R_{n+1} \quad R_n \quad R_{n-1} \quad R_{n-2} \quad \dots \quad R_3 \quad R_2 \quad R_1$$

$$R_1 = a_1$$

$$R_2 = a_2$$

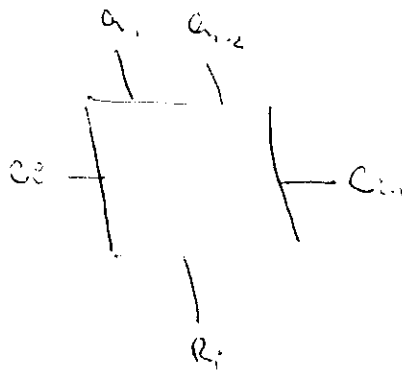
$$R_3 = a_3 + a_1$$

$$R_i = a_i + a_{i+2} + C_{i-1}$$

$$R_n = a_n + a_{n-2} + C_{n-1}$$

$$R_{n+1} = a_{n+1} + C_n$$

$$R_{n+2} = a_n + C_{n+1}$$



a_i	a_{i+2}	C_{i-1}	C_i	R_i
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	0	1
1	0	0	1	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	0

A Karnaugh map for the output R_i is shown below.

$$R_i = a_i \oplus a_{i+2} \oplus C_{i-1}$$

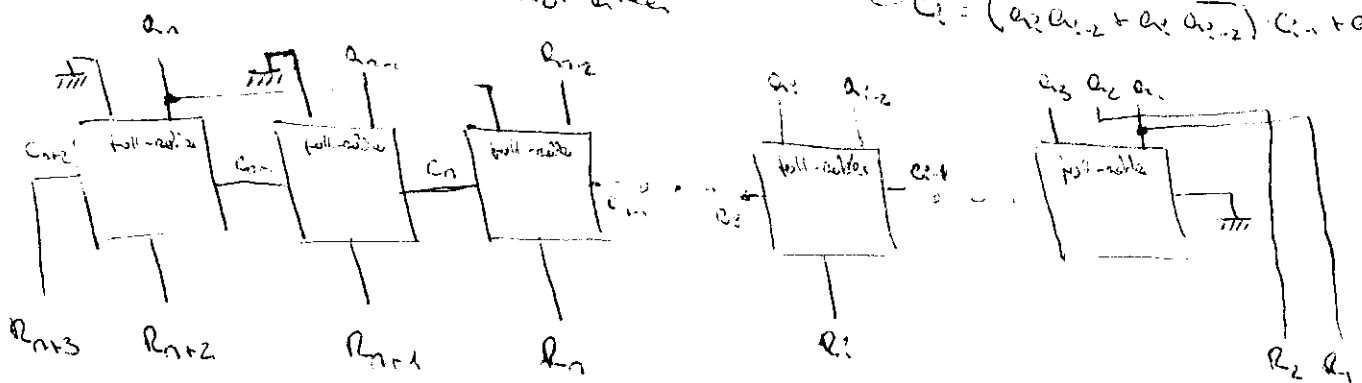
$$C_i = \bar{a}_i a_{i+2} C_{i-1} + a_i \bar{a}_{i+2} C_{i-1} + a_i a_{i+2} \bar{C}_{i-1} + a_i a_{i+2} C_{i-1}$$

$$C_i = \bar{a}_i a_{i+2} C_{i-1} + a_i \bar{a}_{i+2} C_{i-1} + a_i a_{i+2} \bar{C}_{i-1}$$

$$C_i = (\bar{a}_i a_{i+2} + a_i \bar{a}_{i+2}) C_{i-1} + a_i a_{i+2}$$

$$C_i = (a_i \oplus a_{i+2}) C_{i-1} + a_i a_{i+2}$$

Karnaugh map



18)

$$a_1, a_0$$

$$\times b_1, b_0$$

$$a_1 b_1, a_1 b_0, a_0 b_1, a_0 b_0$$

$$a_1 b_1, a_1 b_0, a_0 b_1, a_0 b_0$$

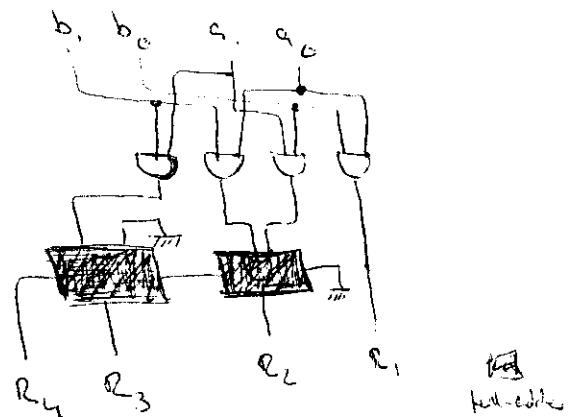
$$R_4, R_3, R_2, R_1$$

$$R_1 = a_0 b_0$$

$$R_2 = a_1 a_0 + a_0 b_1$$

$$R_3 = a_1 b_1 + C_{02}$$

$$R_4 = C_{03}$$



$a_5 \ a_4 \ a_3 \ a_2 \ a_1 \ a_0$

$b_5 \ b_4 \ b_3 \ b_2 \ b_1 \ b_0$

$a_5b_0 \ a_4b_1 \ a_3b_2 \ a_2b_3 \ a_1b_4 \ a_0b_5$

$a_5b_1 \ a_4b_2 \ a_3b_3 \ a_2b_4 \ a_1b_5 \ a_0b_6$

$a_5b_2 \ a_4b_3 \ a_3b_4 \ a_2b_5 \ a_1b_6 \ a_0b_7$

$a_5b_3 \ a_4b_4 \ a_3b_5 \ a_2b_6 \ a_1b_7 \ a_0b_8$

$a_5b_4 \ a_4b_5 \ a_3b_6 \ a_2b_7 \ a_1b_8 \ a_0b_9$

$a_5b_5 \ a_4b_6 \ a_3b_7 \ a_2b_8 \ a_1b_9 \ a_0b_{10}$

$a_5b_6 \ a_4b_7 \ a_3b_8 \ a_2b_9 \ a_1b_{10} \ a_0b_{11}$

$R_8 \ R_7 \ R_6 \ R_5 \ R_4 \ R_3 \ R_2 \ R_1 \ R_0$

$$R_0 = a_0b_0$$

$$R_1 = a_1b_0 + a_0b_1$$

$$R_2 = a_2b_0 + a_1b_1 + a_0b_2$$

$$R_3 = a_3b_0 + a_2b_1 + a_1b_2 + a_0b_3$$

$$R_4 = a_4b_0 + a_3b_1 + a_2b_2 + a_1b_3 + a_0b_4$$

$$R_5 = a_5b_0 + a_4b_1 + a_3b_2 + a_2b_3 + a_1b_4 + a_0b_5$$

$$R_6 = a_5b_1 + a_4b_2 + a_3b_3 + a_2b_4 + a_1b_5 + a_0b_6$$

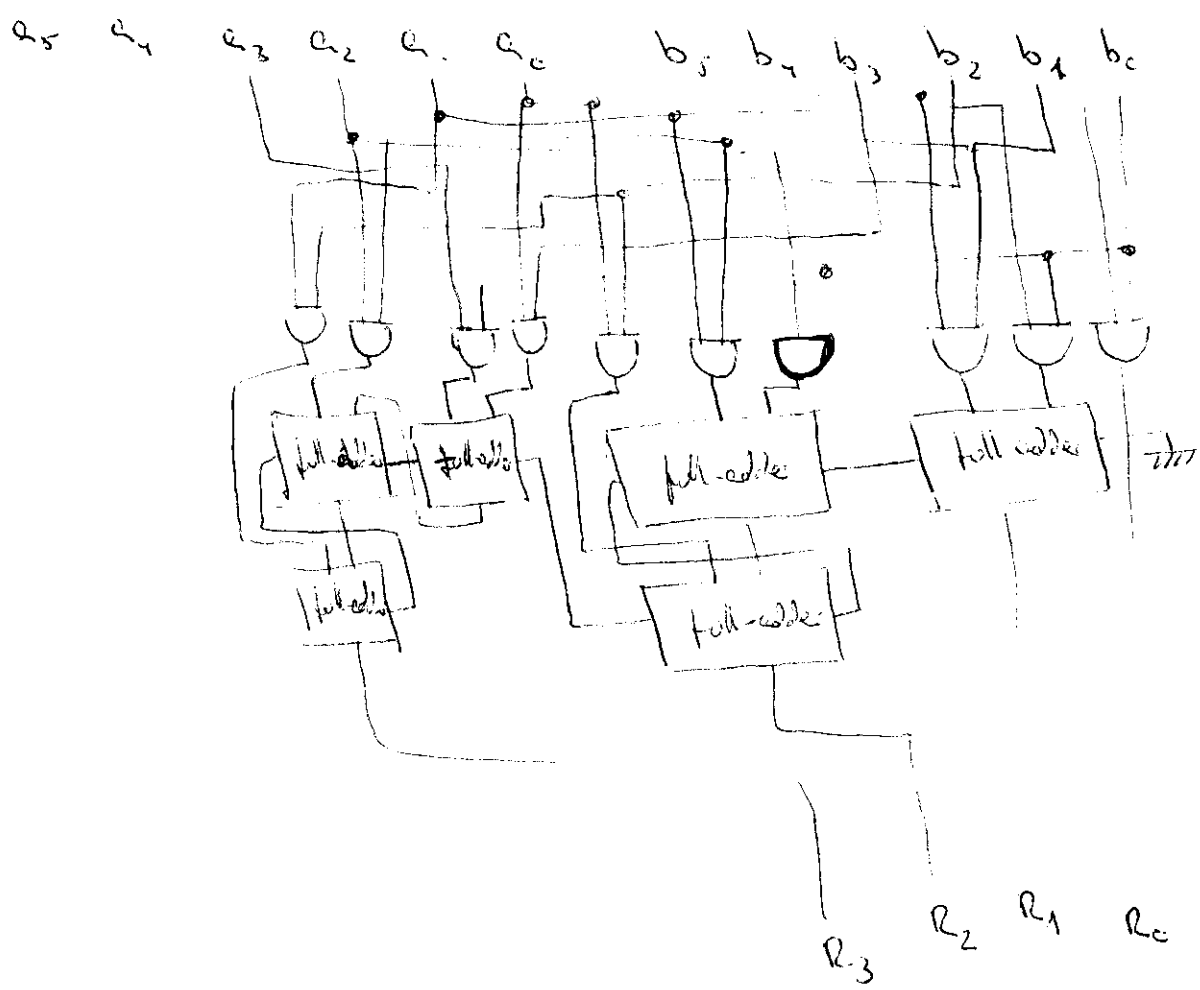
$$R_7 = a_5b_2 + a_4b_3 + a_3b_4 + a_2b_5 + a_1b_6 + a_0b_7$$

$$R_8 = a_5b_3 + a_4b_4 + a_3b_5 + a_2b_6 + a_1b_7 + a_0b_8$$

$$R_9 = a_5b_4 + a_4b_5 + a_3b_6 + a_2b_7 + a_1b_8 + a_0b_9$$

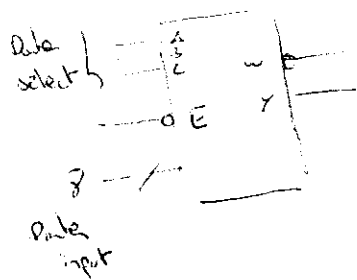
$$R_{10} = a_5b_5 + a_4b_6 + a_3b_7 + a_2b_8 + a_1b_9 + a_0b_{10}$$

$$C_{out}$$



WIKI, SCARDEN TATA (H.C.S.) - 003

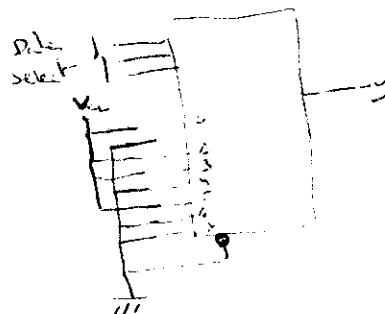
25) 74151 Data $\rightarrow f = \sum m(0, 2, 3, 5)$



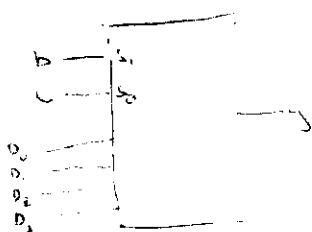
$$Y = D_0 \bar{A} \bar{B} \bar{C} + D_1 \bar{A} \bar{B} C + D_2 \bar{A} B \bar{C} + D_3 \bar{A} B C + D_4 A \bar{B} \bar{C} + D_5 A \bar{B} C + D_6 A B \bar{C} + D_7 A B C$$

$$f = \sum m(0, 2, 3, 5) = \bar{A} \bar{B} \bar{C} + \bar{A} B \bar{C} + \bar{A} B C + A \bar{B} \bar{C}$$

$$\begin{aligned} D_0 &= 1 & D_4 &= 0 \\ D_2 &= 1 & D_5 &= 0 \\ D_3 &= 1 & D_6 &= 0 \\ D_5 &= 1 & D_7 &= 0 \end{aligned}$$



26) 4-to-16 decoder MUX. eqn $f = ab + \bar{b}c$



$$Y = D_0 \bar{a} \bar{b} \bar{c} + D_1 \bar{a} \bar{b} c + D_2 \bar{a} b \bar{c} + D_3 \bar{a} b c$$

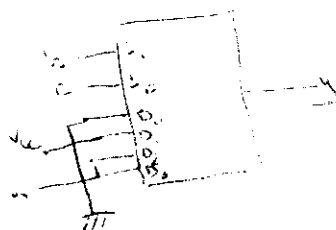
$$f = ab + \bar{b}c$$

$\begin{matrix} a & b & c \\ \downarrow & \downarrow & \downarrow \\ 1 & 0 & 1 \end{matrix}$

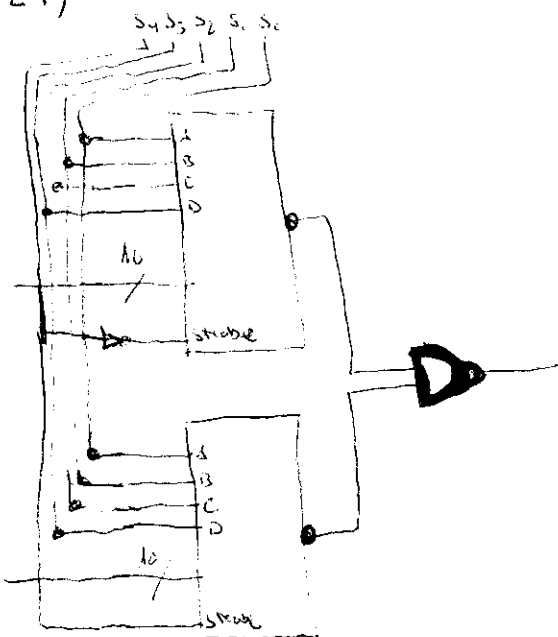
$$f = abc + abc + \bar{b}c$$

$\begin{matrix} \uparrow & \uparrow \\ D_3 & D_2 \end{matrix}$

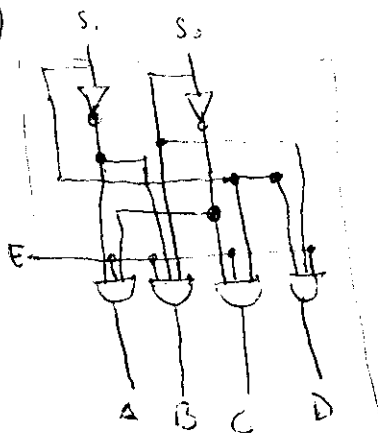
$$\begin{cases} D_3 = a \\ D_2 = a \\ D_1 = 1 \end{cases}$$



24)

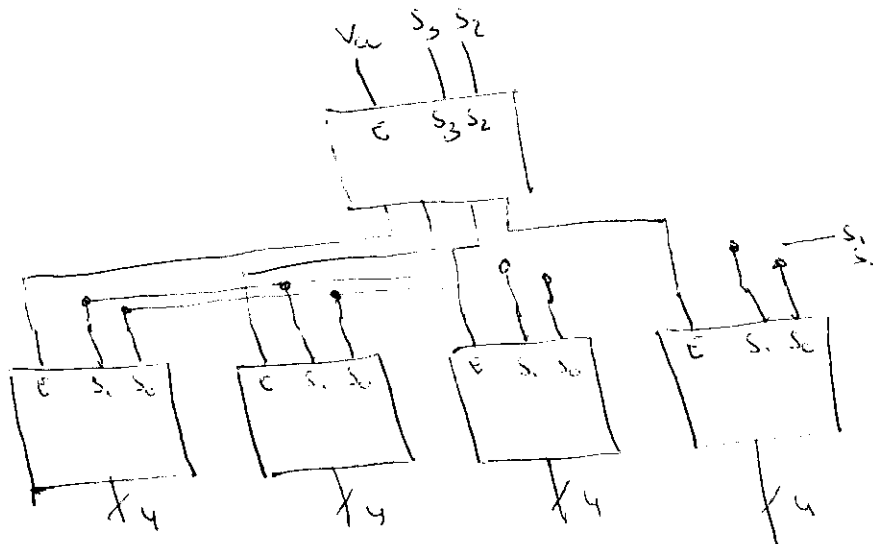


23)



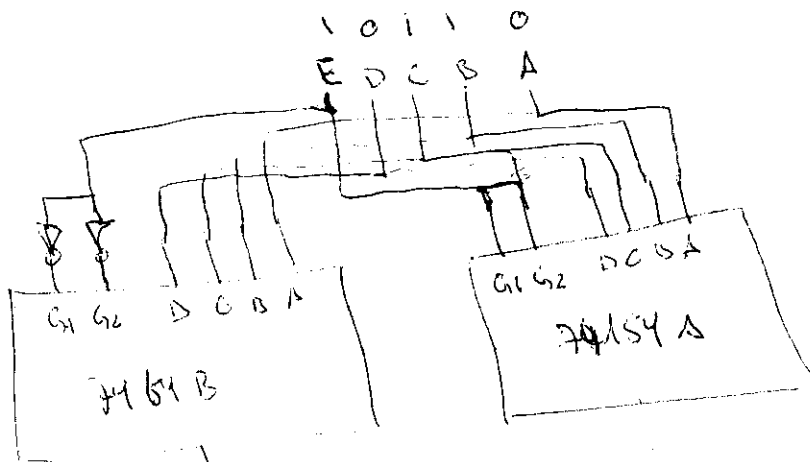
2-4-12

0	0	A	$\overline{S_1} \cdot \overline{S_2}$
0	1	B	$\overline{S_1} \cdot S_2$
1	0	C	$S_1 \cdot \overline{S_2}$
1	1	D	$S_1 \cdot S_2$

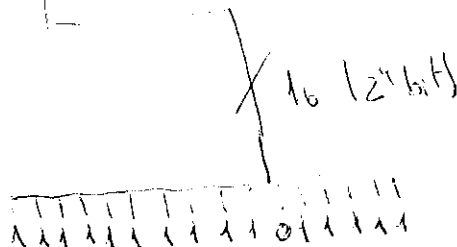


0000	1 2-4
0001	
0010	
0011	
0100	
0101	
0110	
0111	
1000	
1001	
1010	
1011	
1100	
1101	
1110	
1111	

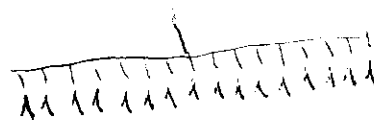
22)



74154 B besitzt 16 Ausgänge
G1, G2, G3, G4, G5, G6, G7, G8, G9, G10, G11, G12, G13, G14, G15, G16



16 (2^4 bits)



30)

$$\begin{aligned}
 & \overline{X_4} \overline{X_3} X_1 \rightarrow \\
 & \overline{X_4} \overline{X_3} X_1 (\overline{C} \overline{B} X_3 + \overline{C} B \overline{X_3} + C \overline{B} \overline{X_3}) \\
 & \overline{X_4} \overline{X_3} X_1 (\overline{C} \overline{B} X_3 + C \overline{B} \overline{X_3}) \\
 & \overline{X_4} \overline{X_3} X_1 (\overline{C} \overline{B} X_3 + \overline{C} B \overline{X_3} + C \overline{B} \overline{X_3}) \\
 & \overline{X_4} \overline{X_3} X_1 (\overline{C} \overline{B} X_3 + C \overline{B} \overline{X_3}) \\
 & \overline{X_4} \overline{X_3} X_1 (\overline{C} \overline{B} X_3 + \overline{C} B \overline{X_3} + C \overline{B} \overline{X_3}) \\
 & \overline{X_4} \overline{X_3} X_1 \\
 & \overline{X_4} \overline{X_3} X_1
 \end{aligned}$$

$$\begin{aligned}
 & C: \overline{X_2} X_0 \\
 & \overline{X_4} \overline{X_3} X_1 + \overline{X_4} \overline{X_3} X_1 + \overline{X_4} \overline{X_3} X_1 + \overline{X_4} \overline{X_3} X_1 + \overline{X_4} \overline{X_3} X_1 + \overline{X_4} \overline{X_3} X_1 \\
 & 000 \quad 001 \quad 010 \quad 011 \quad 100 \quad 101
 \end{aligned}$$